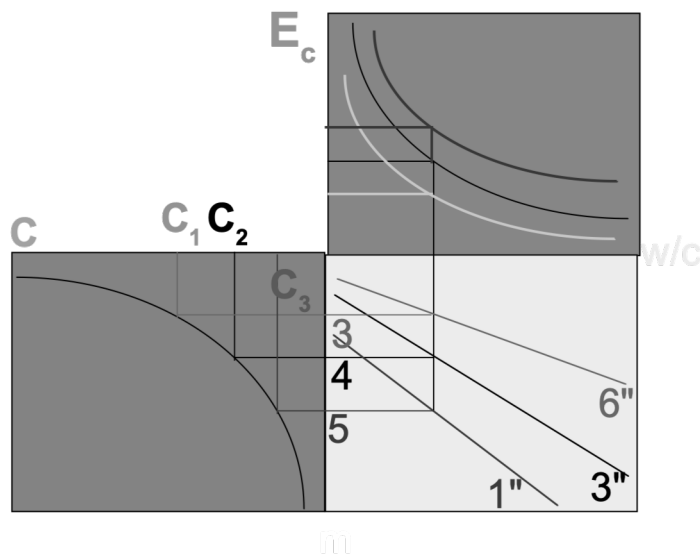


Dosagem do Concreto  
Trevall Powers

Escola Politécnica  
Paulo Helene  
20 de agosto de 2009

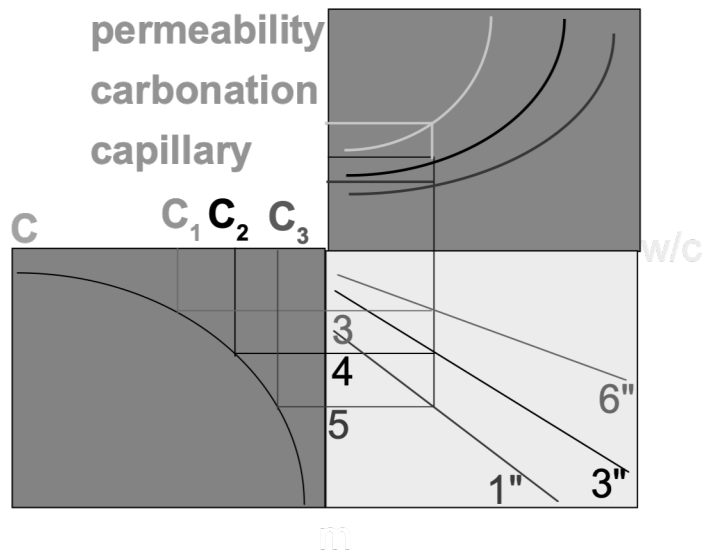
1

**MIX DESIGN NOMOGRAM**



2

## MIX DESIGN NOMOGRAM



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Quais as águas  
da pasta hidratada?



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## Química do Cimento Portland

- $(100) C_3S + (24) H_2O \rightarrow (74) C-S-H + (49) Ca(OH)_2$
- $(100) C_2S + (21) H_2O \rightarrow (100) C-S-H + (21) Ca(OH)_2$
- $(100) C_3A + (30) H_2O \rightarrow \text{etringita} + \text{aluminato}$
- $(100) C_4AF + (37) H_2O \rightarrow \text{aluminato} + \text{ferrito}$
- **compostos menores**

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água capilar

água de gel

água de  
cristalização

6



Qual a água  
necessária para  
hidratar o cimento?

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*cálculo da água de cristalização:*

$C_3S = 51\%$        $C_2S = 23\%$        $C_3A = 8\%$   
 $C_4AF = 9\%$      $CaO \text{ livre} = 1\%$      $CaSO_4 \cdot 2H_2O = 5\%$   
*compostos menores e impurezas = 3%*

$$\begin{array}{l} C_3S \rightarrow 51 \cdot 0.24 = 12 \\ C_2S \rightarrow 23 \cdot 0.21 = 4 \\ C_3A \rightarrow 8 (0.3 \cdot 1.73 + 0.7 \cdot 0.4) = 6 \\ C_4AF \rightarrow 9 \cdot 0.37 = 3 \end{array}$$

*Total  $H_2O = 25 \rightarrow 0.25$  da massa cimento*

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$C_3S \rightarrow 27.6\% \text{ C-S-H} \quad ; \quad 18.4\% \text{ Ca(OH)}_2$

$C_2S \rightarrow 20.8\% \text{ C-S-H} \quad ; \quad 4.3\% \text{ Ca(OH)}_2$

$C_3A \rightarrow \text{estáveis } 3.7\% \quad ; \quad \text{instáveis} = 5.3\%$

$C_4AF \rightarrow \text{estáveis} = 10\%$

**total:**

•  $\text{C-S-H} = 48.8\% \quad \text{estáveis} = 13.7\%$

•  $\text{Ca(OH)}_2 = 22.7\% \quad \text{instáveis} = 5.3\%$

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...a reação de hidratação se dá com redução de volume equivalente a 25.4% do volume de água que reagiu...

cimento = 1 kg

água de cristalização = 0.25 kg

vol. cimento =  $1 / 3.10 = 0.32 \text{ dm}^3$       total  
vol. água cristalização =  $0.25 \text{ dm}^3$        $0.57 \text{ dm}^3$

efetivo  $\rightarrow 0.32 + 0.746 \cdot 0.25 = 0.51 \text{ dm}^3$

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## Powers' Model

gel 100% hidratado

tem 28 % de vazios



para água de  
cristalização = 0.26 →  
água de gel = 0.19 da  
massa cimento

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água mínima para  
hidratação a 100%

cristalização + gel  
→  $0.25 + 0.19 = 0.44$

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## PRINCIPLES



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## POWERS' MODEL

three water : crystallization, chemical or non-evaporable

gel water ( interlayer + adsorbed )

capillary water ( capillary + free )

voids : entrapped air

entrained air

empty pores

capillary water pores

solids products of hydration :

anhydrous cement + chemical water

cement gel :

solid products + gel water

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## POWERS' MODEL

cement paste :

cement gel + capillary water + air + empty pores

porosity of cement gel : etc. ( by volume )

$$\text{gel water} / [ \text{gel water} + \text{solids products} ] = 27 / 28\%$$

volume of solids products of hydration is less than sum of volume of anhydrous cement + chemical water :

contraction equivalent 25.6% of reduction  
of volume the chemical water

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## POWERS' MODEL

1 : 2 : 3 ; 0.55

type of cement :  $C_3S = 50\%$   $C_2S = 22\%$   $C_3A = 13\%$

$C_4AF = 9\%$  others = 6%  $\rightarrow w_{ch} = 0.22$

solid products :

by weight :  $1 + 0.22 = 1.22$

by volume :  $1 / 3.12 + 0.22 / 1.00 = 0.54$  WRONG

$= 0.32 + 0.22( 1 - 0.256 ) = 0.48$  RIGHT

gel water ( from porosity 27% ) :  $w_{gel} = 0.18$

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## POWERS' MODEL

absolute volume of cement =  $1/0.32 = 0.32 \rightarrow 11.6\%$   
 absolute volume of sand =  $2/2.65 = 0.75 \rightarrow 27.1\%$   
 absolute volume of gravel =  $3/2.70 = 1.11 \rightarrow 40.0\%$   
 absolute volume of water =  $0.55/1 = 0.55 \rightarrow 19.8\%$   
 entrapped air =  $1.50\% = 0.04 \rightarrow 1.5\%$

Total volume of concrete = 2.77  $\rightarrow 100\%$

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1 : 2 : 3 ; 0.55		C = 360 kg/m <sup>3</sup> - 600 lb/yd <sup>3</sup>	
FRESH		HYDRATED	
1.5	air = 0.04	air = 0.04	
	w <sub>cap</sub> = 0.15	empty pores 0.06	9.1
19.8	w <sub>gel</sub> = 0.18	w <sub>cap</sub> = 0.15	
	w <sub>ch</sub> = 0.22	w <sub>gel</sub> = 0.18	23.8
11.6	c = 0.32	solid products 0.48	
27.1	s = 0.75	s = 0.75	27.1
40.0	g = 1.11	g = 1.11	40.0
100%	vol.=2.77	vol.=2.77	100%

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**1 : 2 : 3 ; 0.55    C = 360 kg/m<sup>3</sup> - 600 lb/yd<sup>3</sup>**

FRESH		50%		
1.5	<b>air = 0.04</b>		<b>air = 0.04</b>	
	<b>w<sub>cap</sub> = 0.15</b>		empty pores <b>0.03</b>	
19.8	<b>w<sub>gel</sub> = 0.18</b>		<b>w<sub>cap</sub> = 0.35</b>	
	<b>w<sub>ch</sub> = 0.22</b>		<b>w<sub>gel</sub> = 0.09</b>	
11.6	<b>c = 0.32</b>		<b>solid p.=0.24</b>	
	<b>s = 0.75</b>		<b>c = 0.16</b>	
27.1	<b>s = 0.75</b>		<b>s = 0.75</b>	
40.0	<b>g = 1.11</b>		<b>g = 1.11</b>	
<b>100% vol.=2.77</b>			<b>vol.=2.77 100%</b>	

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**1 : 3 : 4 ; 0.55    C = 280 kg/m<sup>3</sup> - 470 lb/yd<sup>3</sup>**

FRESH		HYDRATED		
1.4	<b>air = 0.05</b>		<b>air = 0.05</b>	
	<b>w<sub>cap</sub> = 0.15</b>		empty pores <b>0.06</b>	
15.6	<b>w<sub>gel</sub> = 0.18</b>		<b>w<sub>cap</sub> = 0.15</b>	
	<b>w<sub>ch</sub> = 0.22</b>		<b>w<sub>gel</sub> = 0.18</b>	
9.1	<b>c = 0.32</b>		solid products <b>0.48</b>	
32.0	<b>s = 1.13</b>		<b>s = 1.13</b>	
41.9	<b>g = 1.48</b>		<b>g = 1.48</b>	
<b>100% vol.=3.53</b>			<b>vol.=3.53 100%</b>	

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**1 : 1 : 2 ; 0.55    C = 500 kg/m<sup>3</sup> - 850 lb/yd<sup>3</sup>**

	FRESH		HYDRATED	
<b>1.0</b>	<b>air = 0.02</b>		<b>air = 0.02</b>	
	<b>w<sub>cap</sub> = 0.15</b>		<b>w<sub>cap</sub> = 0.15</b>	
<b>27.4</b>	<b>w<sub>gel</sub> = 0.18</b>		<b>w<sub>gel</sub> = 0.18</b>	
	<b>w<sub>ch</sub> = 0.22</b>		<b>w<sub>gel</sub> = 0.18</b>	
<b>15.9</b>	<b>c = 0.32</b>		<b>solid products</b>	
			<b>0.48</b>	<b>32.8</b>
<b>18.9</b>	<b>s = 0.38</b>		<b>s = 0.38</b>	<b>18.9</b>
<b>36.8</b>	<b>g = 0.74</b>		<b>g = 0.74</b>	<b>36.8</b>
	<b>100% vol.=2.01</b>		<b>vol.=2.01</b>	<b>100%</b>

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**POWERS' MODEL    w/c = cte = 0.55    slump variable**

Mix proportions ( by weight )	Cement content (kg/m <sup>3</sup> ) (lb/yd <sup>3</sup> )	Aggregate s + g	Cement paste	
			cement ge	voids
1 : 1 : 2	500 / 850	55.7%	32.8%	11.5%
1 : 2 : 3	360 / 600	67.1%	23.8%	9.1%
1 : 3 : 4	280 / 470	73.9%	18.7%	7.4%

**How about strength? Permeability? Carbonation? Ions permeability? Creep? Modulus? Drying shrinkage? Durability?**

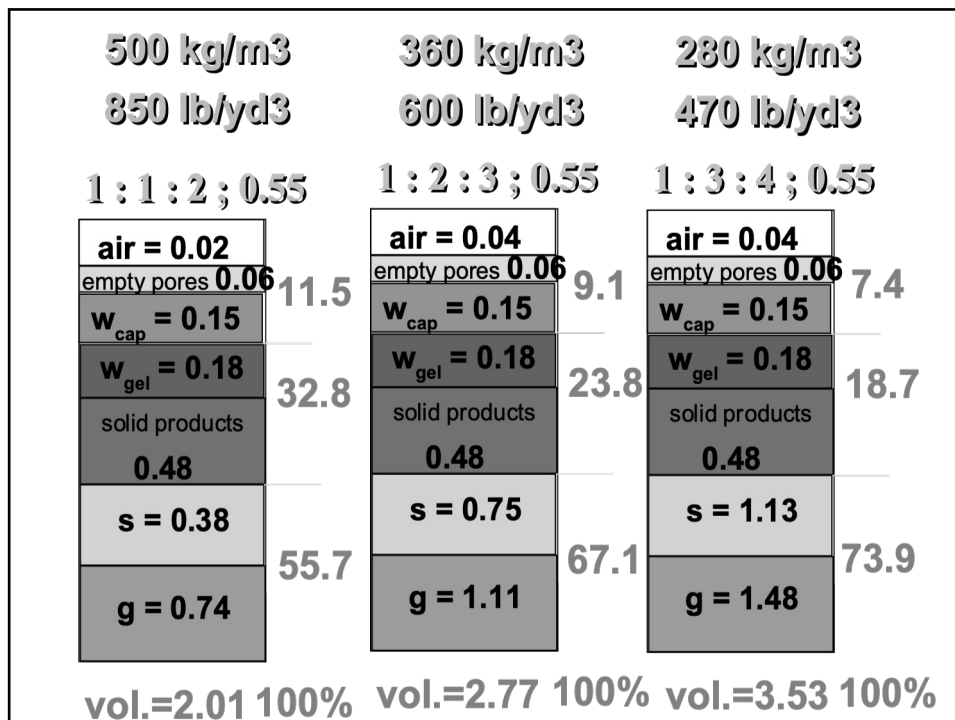
22

**POWERS' MODEL**      **w/c variable**      **slump = cte**

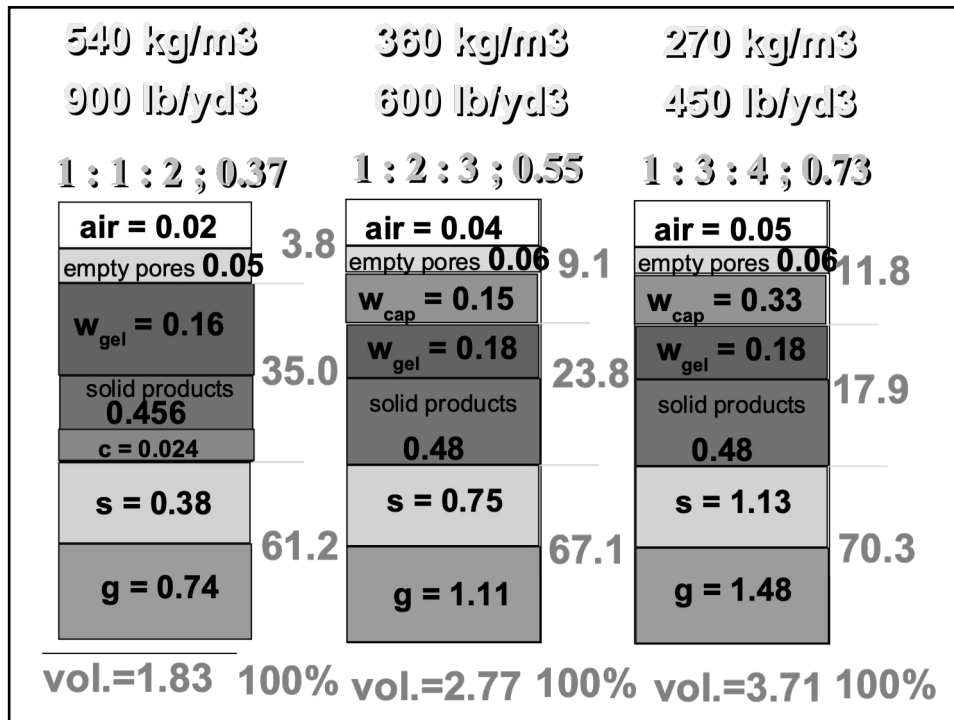
Mix proportions ( by weight )	Cement content (kg/m <sup>3</sup> ) (lb/yd <sup>3</sup> )	Aggregate s + g	Cement paste	
			cement ge	voids
1 : 1 : 2 ; 0.37	540 / 900	61.2%	35.0%	3.8%
1 : 2 : 3 ; 0.55	360 / 600	67.1%	23.8%	9.1%
1 : 3 : 4 ; 0.73	270 / 450	70.3%	17.9%	11.8%

How about strength? Permeability?  
Carbonation? Ions permeability? Creep?  
Modulus?Drying shrinkage?Durability?

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24



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## HISTORY

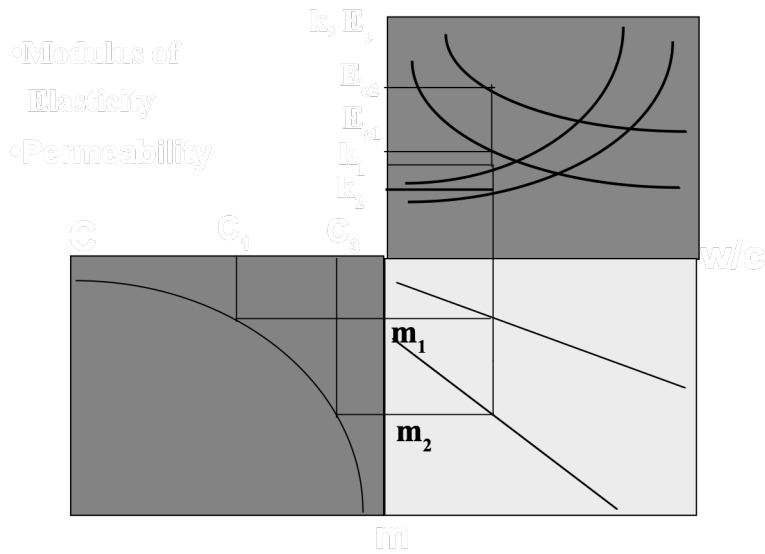
- 1824 -> Joseph Aspdin
- 1896 -> Férèt  

$$f_c = K [ c / ( c+w+air ) ]^2 \text{ (volume)}$$
- 1918 -> Duff Abrams  

$$f_c = K_1 / K_2^{w/c} \text{ ( volume )}$$
  - \*fineness modulus
  - \*slump test

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# MIX DESIGN NOMOGRAM

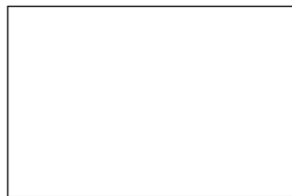


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$w / c = \text{cte}$

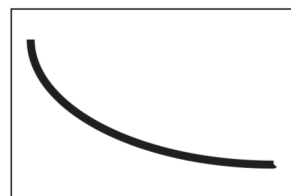
$w / c = \text{variable}$

$c$



aggregates

$f_c$



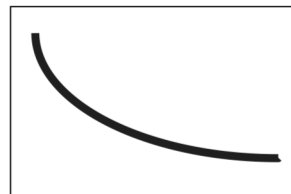
aggregates

$E_c$



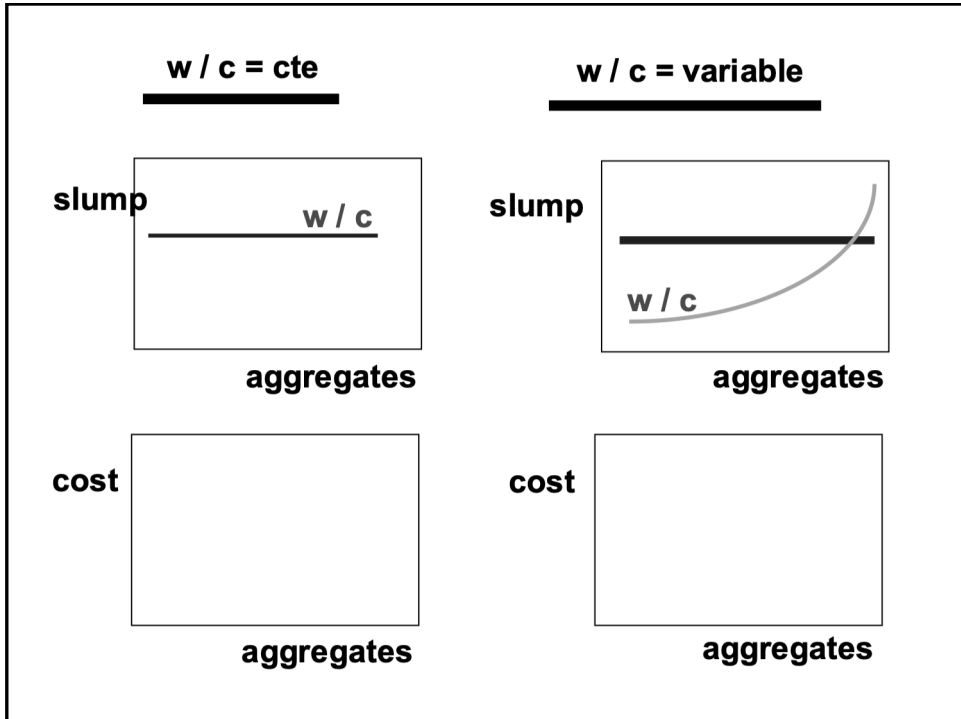
aggregates

$E_c$

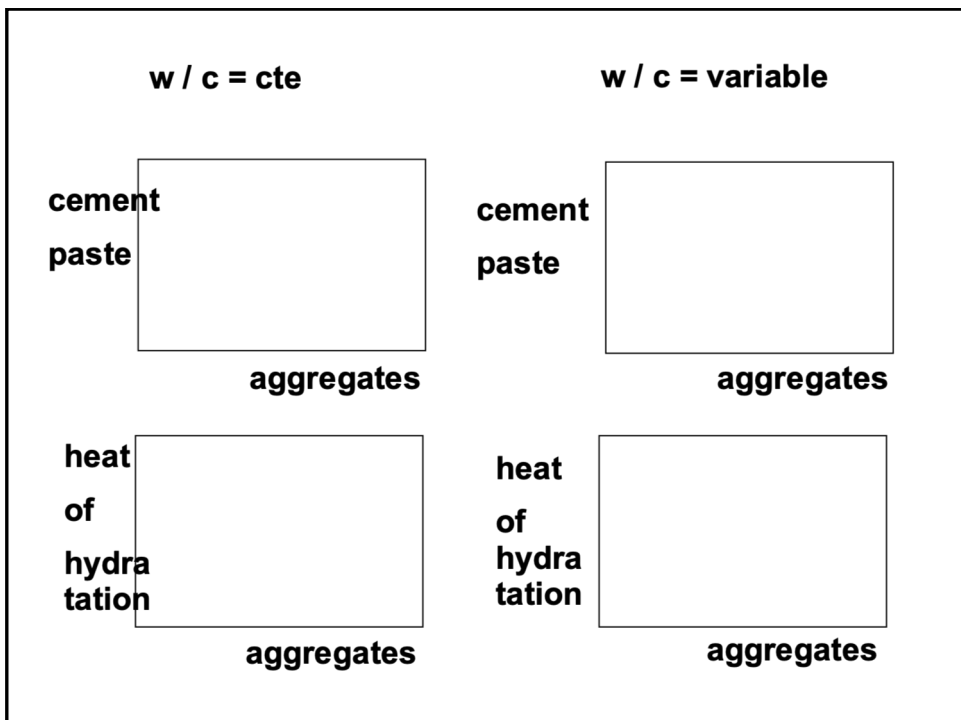


aggregates

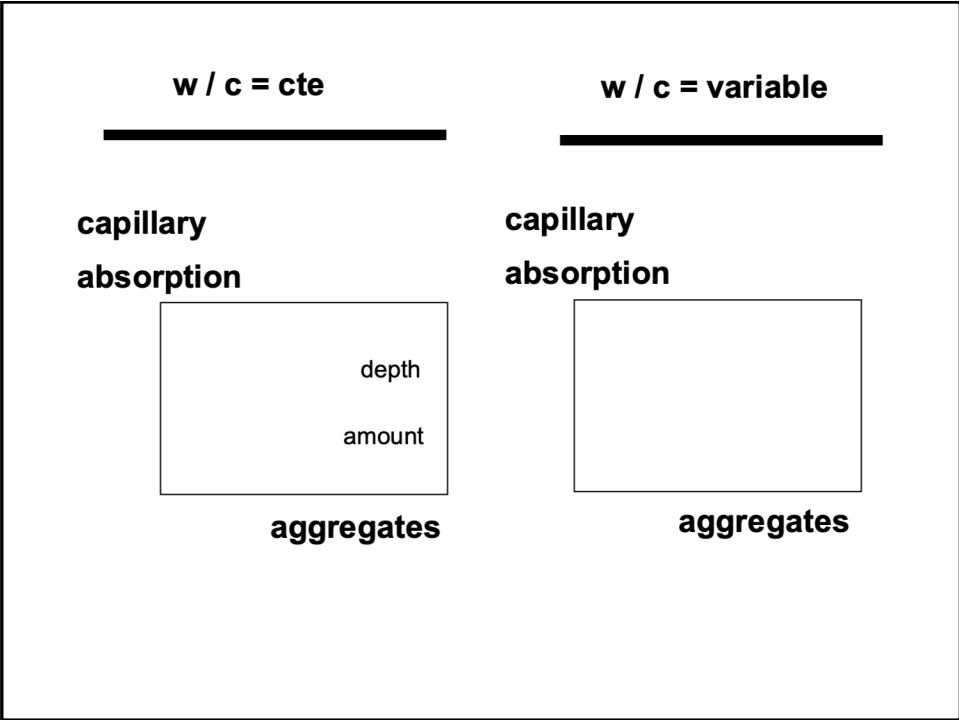
28



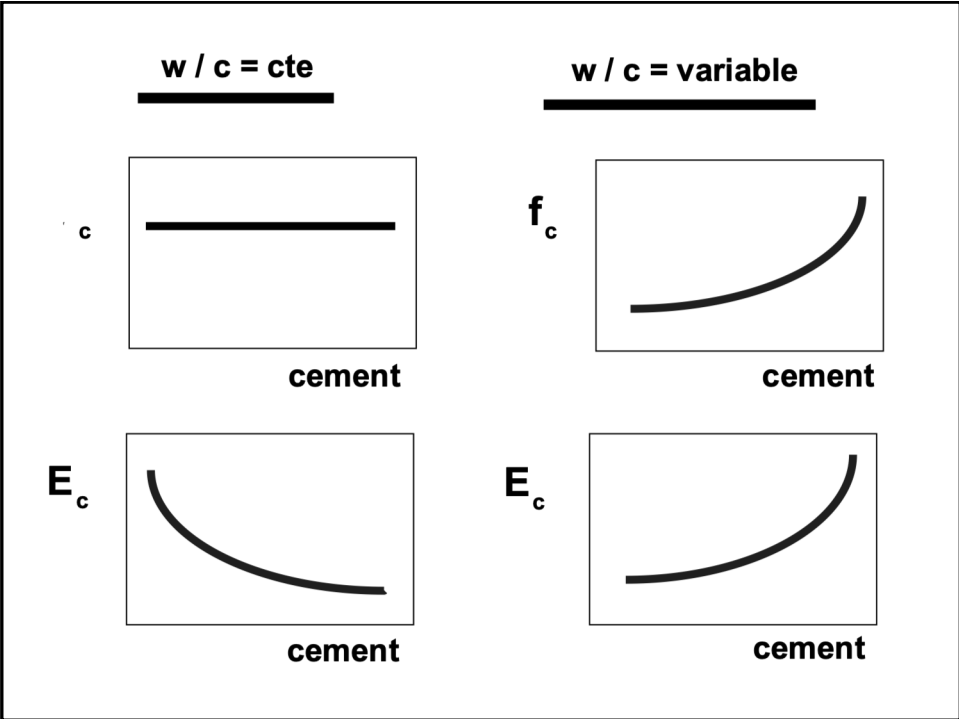
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